A Segmentation-based Method to Extract Structural and Evolutionary Features for Protein Fold Recognition

Abdollah Dehzangi, Kuldip Paliwal, James Lyons, Alok Sharma, Abdul Sattar

Abstract—Protein fold recognition (PFR) is considered as an important step towards the protein structure prediction problem. Despite all the efforts that have been made so far, finding an accurate and fast computational approach to solve the PFR still remains a challenging problem for bioinformatics and computational biology. In this study, we propose the concept of segmented-based feature extraction technique to provide local evolutionary information embedded in Position Specific Scoring Matrix (PSSM) and structural information embedded in the predicted secondary structure of proteins using SPINE-X. We also employ the concept of occurrence feature to extract global discriminatory information from PSSM and SPINE-X. By applying a Support Vector Machine (SVM) to our extracted features, we enhance the protein fold prediction accuracy for 7.4% over the best results reported in the literature. We also report 73.8% prediction accuracy for a data set consisting of proteins with less than 25% sequence similarity rates and 80.7% prediction accuracy for a data set with proteins belonging to 110 folds with less than 40% sequence similarity rates. We also investigate the relation between the number of folds and the number of features being used and show that the number of features should be increased to get better protein fold prediction results when the number of folds is relatively large.

Index Terms—Protein Fold Recognition, Feature Extraction, Structural-based Features, Evolutionary-based Features, Segmented distribution, Segmented Auto Covariance, Occurrence, Support Vector Machine (SVM)

A Protein consists of a sequence of monomers called amino acids that are connected to each other through peptide bonds. Proteins are considered as the most important biological micro-molecules and play a vital role in most of the biological interactions. Therefore, determining how it functions is an important task in biology and biomedical science. Protein Fold Recognition (PFR) is considered as an important step towards protein function prediction. PFR is defined as assigning a given protein to a fold (among a finite number of folds) that represents its functionality as well as its major tertiary structure. Despite all the efforts that have been made during the last two decades, finding an effective computational approach to solve this problem still remains crucial for computational biology and bioinformatics [1]. In the pattern recognition terminology, the PFR is defined as solving a multi-class classification task in which its performance is crucially relied on the features and classification techniques being used. Features that capture significant global and local discriminatory information and the classification techniques that perform consistently with these extracted features have been used in the literature [2]. A wide range of classification techniques such as, Artificial Neural Networks (ANN) [3], [4], [5], [6], [7], [8], Meta Classifiers [9], [10], [11], [12], [13], K-Nearest Neighbors [14], [15], [16], [17], [18] and Support Vector Machines (SVM) [19], [20], [21], [22], [23], [24], [25], [26], [27] have been used for the PFR. Among the classifiers employed to tackle the PFR, using Support Vector Machine (SVM) have attained the best results [26], [27], [28], [29], [30], [31], [32]. Similarly, a wide range of features have been extracted and used to tackle the PFR such as, Physicochemical-based features [19], [23], [33], [34], Sequence-based features [6], [14], [15], [32] Evolutionary-based features [18], [25], [28], [30], and Structural-based features [17], [18], [23], [35], [36], [37], [38]. Achieved results have shown that the most significant enhancement for the protein fold prediction accuracy has been achieved by relying on the feature extraction approaches rather than the classification techniques being used [4], [15], [19], [27], [28], [29], [39]. In most of the studies that addressed the PFR by feature extraction techniques, global discriminatory information has been represented using the composition of the amino acids feature group (the percentage of the occurrence of the amino acids along the protein sequence divided by the length of protein sequence [19], [22], [30]). However, it has been shown that this feature group is not able to adequately reveal global information as it is not able to...
capture information regarding the length of the protein sequence [39], [40] which was shown as effective feature for the PFR [33], [41].

Compared to the methods adopted to extract global discriminatory information, a wider range of methods were used to extract local discriminatory information for the PFR [42] such as, pseudo amino acid composition [14], [15], [22], [23], [43], cross covariance [28], auto covariance [28], [42], bi-gram [29], [39], and tri-gram [3]. Despite the significant local discriminatory information provided using these approaches, most of these methods produce large number of features as well as large amount of redundant features [14], [29] which makes them computationally expensive for large protein data banks (e.g. cross covariance and tri-gram [3], [28]). At the same time, in all these methods the whole protein sequence as a single entity have been used to extract local information. In other words, they aimed to extract local information by exploring whole protein sequence as a global entity [17], [28]. Therefore, they could not appropriately explore local information embedded in protein sequence [33], [40]. As a results, the protein fold prediction accuracy remains limited especially when the sequence similarity rate is low [39].

In this study, we aim at enhancing protein fold prediction accuracy by addressing these limitations. We propose a segmentation-based feature extraction method to extract local evolutionary information embedded in Position Specific Scoring Matrix (PSSM) as well as structural information embedded in the predicted secondary structure using SPINE-X. In this method, we divide the protein sequence into several segments and extract distribution and auto-covariance features from each segment. We also employ the concept of an occurrence feature of the transformed protein sequence using evolutionary and structural information embedded in PSSM and SPINE-X to extract adequate global discriminatory information for the PFR. We investigate the impact and generality of our proposed methods on four data sets including a data set consisting of proteins with less than 25% sequence similarity and a data set consisting of proteins belonging to 110 different folds with less than 40% sequence similarity. By applying SVM to our extracted features we enhance the protein fold prediction accuracy by 7.4% better than the highest reported results found in the literature.

1 DATA sets

In this study, four data sets namely TG, EDD, F92, and F110 are used to investigate the performance of our proposed methods. The TG data set introduced by [40] consists of 1612 proteins belonging to 30 folds with less than 25% sequence similarities. TG is extracted from Structural Classification of Proteins (SCOP) 1.73 which has been previously used to investigate the performance of proposed methods for the PFR when the sequence similarity is very low [33], [40], [44]. We also extract EDD (extended version of DD data set [19] which is extracted from SCOP 1.75). This data set consists of 3418 proteins belonging to 27 folds that was used originally in DD data set with less than 40% sequence similarities. The EDD data set extracted from an older version of SCOP has been widely used for the PFR [21], [28], [29]. This data set enables us to directly compare our results with previously reported results found in the literature.

To investigate the impact of our proposed methods for more complex (regarding to the number of folds containing in the data set) data sets consisting of larger number of folds, we have extracted two new data sets namely F92 and F110 from the SCOP 1.75. F92 data set consists of 6331 proteins belonging to 92 most populated folds in SCOP. This data set is generated by making sure that each fold at least consists of 25 proteins. The F110 contains 6723 proteins belonging to 110 folds in which each fold has more than 20 proteins. Having larger number of folds, these two data sets are able to provide more reliable and general results for the PFR. Furthermore, comparison of the results achieved for the EDD, F92, and F110 can provide important information regarding the impact of increasing the number of folds and consequently complexity of the problem on the PFR performance. These four data sets are available upon request.

2 FEATURE EXTRACTION METHOD

In this study, we rely on PSSM and the predicted secondary structure using SPINE-X to extract evolutionary and structural information respectively. PSSM is calculated by applying PSIBLAST [45] to EDD and TG data sets (using NCBI’s non redundant (NR) database with its cut off value (E) set to 0.001). PSSM consists of an $L \times 20$ matrix ($L$ is the length of a protein and the columns of the matrices represent 20 amino acids). It provides the substitution probability of a given amino acid based on its position along a protein sequence. Extracted features from PSSM have been widely used for the PFR and attained promising results [27], [28], [29].

We also use predicted secondary structure using SPINE-X which was recently proposed by [46] and attained better results (especially for the coded area) than PSIPRED on predicting protein secondary structure [47]. Given a protein sequence, it returns an $L \times 3$ matrix (which will be referred to as SPINE-M for the rest of this study) consisting of the normalized probability of contribution of a given amino acid based on its position along the protein sequence to build one of the three secondary structure elements namely, α-helix, β-strands, and coils. It also returns a transformed version of the protein sequence (also extracted from SPINE-M) in which each amino acid along the protein sequence is replaced with $H$ (represents helix), $E$ (represents strand), or $C$ (represents coil) based on its tendency to incorporate in building one of these secondary structure elements. In this study, we will refer to this sequence as the structural consensus sequence. It is expected that predicted secondary
structure using SPINE-X provides significant structural information for the PFR similar to or even better than PSIPRED due to its better performance [17], [23], [30], [46].

During the last decade, the substitution score (extracted from the PSSM) and predicted secondary structure using PSIBLAST and SPINE-X (or PSIPRED before that) have been widely used in protein science (e.g. protein fold recognition, protein function prediction, protein structure prediction, protein subcellular localization) and extracted features from these sources attained promising results [23], [28], [30], [38], [42], [48]. As it is highlighted in [49], the most successful methods for fold recognition use sequence profiles to represent both the query and the data base proteins. The robustness and sensitivity of PSSM and SPINE-X for feature extraction have been addressed in [23], [46], [49]. In continuation, the global and local features extracted in this study will be explained in detail. The SPINE-M and PSSM for all four data sets used in this study are available upon request.

2.1 Global Features

To extract global discriminatory information embedded in PSSM and SPINE-M we mainly relied on the concept of the occurrence feature. We extract evolutionary and structural consensus sequence-based occurrence from the transformed protein sequence using PSSM and SPINE-M respectively. We also extract semi-occurrence feature group directly from PSSM and SPINE-M which represents the summation of the substitution probability of the amino acids and normalized probability of the secondary structure elements, respectively.

2.1.1 Consensus Sequence-based Occurrence:

In this method, we extract occurrence of the amino acids as well as occurrence of the secondary structure elements derived from the evolutionary-based and the structural-based consensus sequences, respectively. To extract the occurrence feature group from the evolutionary consensus sequence, we first need to extract this sequence from PSSM. In the evolutionary consensus sequence, amino acids along the original protein sequence \(O_1, O_2, \ldots, O_L\) are replaced with the corresponding amino acids with the maximum substitution probability \(C_1, C_2, \ldots, C_L\). This is done in the following two steps. In the first step, for a given amino acid, the index of the amino acid with the highest substitution probability is calculated as follows:

\[
I_i = \arg\max \{ P_{ij} : 1 \leq j \leq 20 \}, \quad 1 \leq i \leq L, \tag{1}
\]

where \(P_{ij}\) is the substitution probability of the amino acid at location \(i\) with the \(j^{th}\) amino acid in PSSM. In the second step, we replace the amino acid at \(i^{th}\) location of original protein sequence by the \(I_i^{th}\) amino acid to form the consensus sequence. After calculating the evolutionary consensus sequence, we count the occurrence of each amino acid (for all the 20 amino acids) along this sequence and produce the occurrence feature from the evolutionary based consensus sequence which we call (AAO). Similarly, we calculate the occurrence of each secondary structure elements (SSEO) (for all three elements) in the structural consensus sequence and extract the corresponding feature group. The occurrence feature group is used in this study as the global descriptor of the proteins since it maintains the information regarding the length of protein sequence which is disregarded using composition feature group [21], [23], [50].

2.1.2 Semi-Occurrence:

In this method, we calculate semi-occurrence feature group from both PSSM and SPINE-M. It is called semi-occurrence because instead of using the protein sequence directly to calculate the occurrence of each amino acid, we calculate the summation of the substitution probability for each amino acid from the PSSM or normalized frequency of each secondary structure element from SPINE-M. The semi-occurrence derived from the PSSM (PSSM-AAO) is calculated as follows:

\[
PSSM-AAO = \sum_{i=1}^{L} P_{ij}, \quad (j = 1, \ldots, 20). \tag{2}
\]

In a similar manner, we calculate the semi-occurrence of the normalized frequency of the secondary structure elements from SPINE-M (SPINE-SSEO) as follows:

\[
SPINE-SSEO = \sum_{i=1}^{L} S_{ij}, \quad (j = 1, 2, 3), \tag{3}
\]

where \(S_{ij}\) is the normalized probability of the occurrence of the \(j^{th}\) secondary structure element for the \(i^{th}\) amino acid in the SPINE-M. These feature groups are able to provide important global discriminatory information about the substitution probability of the amino acids as well as normalized frequency of secondary structure elements based on PSSM and SPINE-M. For the rest of this study, the combination of all these four global feature groups (AAO + SSEO + PSSM-AAO + SPINE-SSEO) will be referred as \(F_{global}\) (consisting of 46 features in total).

2.2 Local Features

To extract these features, we use a segmentation method described below and extract distribution and auto covariance features from the individual segments. In this manner, we are able to provide more local information compared to the global features described earlier.

2.2.1 Segmented Distribution Features:

Here, we first apply a segmentation method to individual columns of PSSM and SPINE-M matrices, and represent each segment by a distribution feature. For PSSM, for the \(j^{th}\) column, we first calculate the total sum of substitution probability \(T_j = \sum_{i=1}^{L} P_{ij}\). Then, starting from the first row of PSSM (which corresponds to the
first amino acid in the protein sequence), we compute the sum \( S_1 = \sum_{i=1}^{I_1} P_{ij} \) of the substitution probabilities corresponding to the \( j^{th} \) column until reaching to less than or equal to \( F_P \) (segmentation factor) of \( T_j \), where \( I_1 \) is the number of amino acids used in computing the sum \( S_1 \). The amino acids from index 1 to \( I_1 \) are considered to define the first segment for the \( j^{th} \) column of the PSSM. We use the index of last amino acid of this segment (i.e., \( I_1 \)) as the first segmented distribution feature. Next, we calculate the index of the last amino acid in the second segment (i.e., \( I_2 \)) by summing the substitution probability of amino acids (again, starting from the first row of PSSM) until reaching \( 2 \times F_P \) of \( T_j \), and use it as second segmented distribution feature. In this study, \( F_P \) is set to 25% as other values of \( F_P \) (10% and 5%) attained similar performance.

Next, we calculate two more features \( (I_3^j, I_4^j) \) for the \( j^{th} \) column of PSSM by carrying out the segmentation in reverse order. Instead of starting from the first row of \( j^{th} \) column of PSSM as done previously to compute \( I_1 \) and \( I_2 \), we now start from the last row of PSSM (corresponding to the last amino acids of the protein sequence). To compute \( I_3^j \), starting from the last row of PSSM, we sum the substitution probabilities of amino acids until reaching less than or equal to \( F_P \) of \( T_j \). In the similar manner, we calculate \( I_4^j \), summing substitution probability of amino acids (starting from the last row of PSSM) until reaching to \( 2 \times F_P \) of total sum (\( T_j \)). Thus, we calculate 4 segmented distribution features for each column in PSSM. This means that we will have a total of \( 4 \times 20 = 80 \) features for 20 columns in PSSM to build segmented distribution feature group (called PSSM SD). The configuration of the segmentation scheme adopted in this study is shown in Figure 1.

In a similar manner, we calculate the segmented distribution feature group of the normalized frequency of the secondary structure elements from SPINE-M (called SPINE SD) using \( F_S = 25\% \) (where \( F_s \) is used as the distribution factor for SPINE-M equivalent to \( F_P \) used for PSSM) and respectively extract \( 3 \times 4 = 12 \) features in total for all three elements. In segmentation-based distribution feature extraction technique, we extract the distribution factor in which explains how amino acids are distributed along protein sequence with respect to their substitution scores. Therefore, it returns the index which is equal to the number of amino acids for each segment while semi-occurrence returns the summation of substitution scores. The distribution factor has been shown as effective features which it’s emphasized as well in this study [19].

### 2.2.2 Segmented Auto Covariance Features:

The concept of auto covariance has been widely used in the literature to capture local discriminatory information and has attained better results compared to bi-gram [29], [39] or tri-gram features [3]. Pseudo amino acid composition based features are good examples of these types of features [14], [17]. These features have been computed using the whole protein sequence as a single entity for feature extraction. Therefore, they could not adequately explore the local discriminatory information embedded in protein sequence [28]. In the present study, we extend the concept of segmented distribution features as described in the previous subsection to compute the auto covariance features. This provides more local evolutionary and structural information from PSSM and SPINE-M. First for PSSM, we segment the protein sequence using \( F_P = 25\% \). Using a procedure similar to the one described in the previous subsection, for the \( j^{th} \) column in PSSM we divide the protein sequence into 4 segments (from first amino acid corresponding to first row of PSSM until reaching \( I_1 \)); from first amino acid corresponding to first row of PSSM until reaching \( I_2 \); from last amino acid corresponding to the last row of PSSM until reaching \( I_3 \); and from last amino acid corresponding to the last row of PSSM until reaching \( I_4 \)). we calculate auto covariance feature using \( K_P \) (distance factor used for PSSM for each segment) as follows:

\[
P^{\text{seg}}_{\theta,m,j} = \frac{1}{(L-m)} \sum_{i=1}^{l \equiv \sum_{i=1}^{L-m} (P_{i,j} - P_{\text{ave},j}) \times (P_{(i+m),j} - P_{\text{ave},j})},
\]

where \( P_{\text{ave},j} \) is the average substitution probability for the \( j^{th} \) column in PSSM. We also compute the global auto covariance coefficient (\( K_P \) features) as follows:

\[
P^{\text{AC}}_{\theta,m,j} = \frac{1}{(L-m)} \sum_{i=1}^{l \equiv \sum_{i=1}^{L-m} (P_{i,j} - P_{\text{ave},j}) \times (P_{(i+m),j} - P_{\text{ave},j})},
\]

Thus, we extract a total of \( (2K_P + 2K_P + K_P) \) auto covariance features (\( 2K_P \) features for segments corresponding to \( I_1 \) and \( I_2 \), \( 2K_P \) features for segments corresponding to \( I_3 \) and \( I_4 \) and \( K_P \) features corresponding to global auto covariance) in this manner. Then by combining PSSM-AC and PSSM-seg (extracted for all 20 columns of PSSM) we build the corresponding feature.
group which is called PSSM-SAC \((20 \times (5 \times K_p))\) features in total.

This procedure is also repeated for SPINE-M in the same way \((K_s)\) is used as the distance factor for SPINE-M equivalent to \(K_p\) used for PSSM) for all three columns of SPINE-M and segmented auto covariance of normalized frequency of secondary structure elements are extracted as follows:

\[
\text{SPINE-seg}_{m, j} = \frac{1}{(L - m)} \sum_{i=1}^{L-m} (S_{i,j} - S_{\text{ave},j}) \times (S_{(i+m),j} - S_{\text{ave},j}),
\]

\[(n = 1, 2, 3, 4 \& m = 1, ..., K_s \& j = 1, 2, 3).
\]

where, \(S_{\text{ave},j}\) is the average substitution probability for the \(j^{th}\) column in SPINE-M. Similarly, the global auto covariance is computed as follows:

\[
\text{SPINE-AC}_{m, j} = \frac{1}{(L - m)} \sum_{i=1}^{L-m} (S_{i,j} - S_{\text{ave},j}) \times (S_{(i+m),j} - S_{\text{ave},j}),
\]

\[(m = 1, ..., K_s \& j = 1, 2, 3).
\]

The combination of SPINE-seg and SPINE-AC builds SPINE-SAC consisting of \(3 \times (5K_s)\) features in total (extracted for all three columns of SPINE-M).

3 SUPPORT VECTOR MACHINE

In pattern recognition, SVM is considered as the state-of-the-art classification technique. It was introduced by [51] aiming at finding the Maximum Margin Hyperplane (MMH) based on the concept of support vector theory to minimize classification error. It transforms the input data to higher dimensionality using the kernel function to find support vectors. The classification of some known points in input space \(x_i\) is \(y_i\), which is defined to be either -1 or +1. If \(x^\prime\) is a point in input space with unknown classification then:

\[
y^\prime = \text{sign}\left(\sum_{i=1}^{n} a_i y_i K(x_i, x^\prime) + b\right),
\]

where \(y^\prime\) is the predicted class of point \(x^\prime\). The function \(K()\) is the kernel function; \(n\) is the number of support vectors and \(a_i\) are adjustable weights and \(b\) is the bias. Among a wide range of complex classification techniques used for the PFR [5], [16], [20], [52], [53], the best results reported in the literature was attained using this classifier [28], [29], [30]. In this study, the SVM classifier implemented in LIBSVM (C-SVC type and using one-versus-one approach to extend it for multi-class classification task) toolbox with Radial Basis Function (RBF) as its kernel function is used [54]. RBF kernel is adopted here due to its better performance than other kernels functions (e.g. polynomial kernel, linear kernel, and sigmoid [28]). In this study, the width parameter \(\gamma\) in addition to the cost parameter \(C\) of the SVM are optimized using grid search algorithm implemented in the LIBSVM package. The grid search algorithm tries various pairs of \(\gamma\) and \(C\) values and selects the values with the best classification accuracy [54].

4 RESULTS AND DISCUSSION

We construct the input feature vector to use with SVM consisting of our extracted feature \((F_{\text{global}} + \text{PSSM-SD} + \text{SPINE-SD} + \text{PSSM-SAC} + \text{SPINE-SAC})\). The architecture of our proposed system is shown in Figure 2.

To evaluate the performance of our proposed methods, 10-fold cross validation evaluation criterion is adopted in this study as it was mostly used for this task in the literature [19], [21], [29], [40]. We first investigate the impact of our proposed method for the PFR with respect to the \(K_p\) and \(K_s\) parameters in PSSM-SAC and SPINE-SAC respectively. Then we investigate the impact of each of the proposed feature groups in this study separately on the achieved prediction accuracy. Finally, we compare our achieved results with previously reported results for the PFR.

4.1 Investigating the Impact of \(K_p\) and \(K_s\)

As it was mentioned earlier, \(K_p\) and \(K_s\) values between 1 and 10 are investigated here (since it was shown in [28] that using a distance factor larger than 10 to extract auto covariance feature group attains similar results with using 10 for the PFR). To do this, in 10 different experiments, we apply SVM to our proposed feature vector while \(K_p\) and \(K_s\) are monotonically increased from 1 to 10 \((K_p = 1 \& K_s = 1, K_p = 2 \& K_s = 2, ..., K_p = 10 \& K_s = 10)\). The results for this experiment is shown in Figure 3.

We also calculate the SVM parameters on the EDD data set \((K_p = 10 \& K_s = 10)\) for our proposed feature vector using the grid search algorithm. Calculated parameters are used for the rest of this study (to avoid over tuning parameters) for all four data sets used in this study \((C = 0.075 \& \gamma = 100)\). We have also conduct the parameter tuning for the F92 data set in which attained to its best results with the same parameters extracted for the EDD. Note that the TG and F110 data sets have not been used at all for parameter tuning.

As we can see, increasing the \(K_p\) and \(K_s\), prediction accuracy almost monotonically increases as well. Using \(K_p = 10 \& K_s = 10\), we reach to 88.1\%, 73.1\%, 81.2\%, and 80.4\% prediction accuracies for the EDD, TG, F92, and F110 data sets respectively. However, it is not clear which one of \(K_p\) and \(K_s\) has the main impact on the achieved results. Furthermore, the impact of increasing \(K_p\) and \(K_s\) on the EDD and TG data sets are slightly different from F92 and F110. As it is shown in Figure 3, increasing \(K_p\) and \(K_s\), from 1 to 10, the prediction accuracy almost monotonically increases for the EDD and TG data sets while for the F92 and F110, it monotonically increase until \(K_p = 7\) and \(K_s = 7\) and then it remains unchanged (and slightly drops). Having significantly different number of folds in the F92 and F110, it is expected that addressing the PFR using
Fig. 2: The general architecture of our proposed feature extraction model. The number of features extracted in each feature group is shown in the brackets below the feature groups’ names.

Fig. 3: The results achieved for EDD, TG, F93, and F110 data sets with respect to $K_p$ and $K_s$ which are monotonically increase from 1 to 10.

these two data sets would be more complex and slightly different from the EDD and TG.

Therefore, we investigate the impact of $K_p$ and $K_s$ for two cases. We first investigate the impact of these two parameters on the EDD and TG data sets and then for the F92, and F110 data sets, separately. To investigate the effectiveness of $K_p$ and $K_s$ on the EDD data set (then explore the impact on the TG data set), two different experiments are conducted. First, we set the value of $K_p = 1$ and in 10 different experiments, increase the value of $K_s$ from 1 to 10 (Figure 4.a). As we can see, increasing $K_s$ monotonically increases the prediction accuracy and setting $K_s = 10$ attain the best result for this task. In a different experiment, we set the value of $K_s = 10$ (since the best results attained by adjusting $K_s = 10$) and in 10 different experiments, increase the value of $K_p$ from 1 to 10. As we can see in Figure 4.b, the performance does not change by increasing the $K_p$. As it is shown in the Figures 4.a and 4.b, similar results are achieved for the TG data set. In other words, using segmented auto covariance approach, we are able to reveal more local discriminatory information from PSSM and SPINE-M based on the concept of auto covariance compared to previous studies ($K_p = 1$ and $K_s = 10$). Note that this number of features is dramatically lower than the number of features used in [28] and [29] to enhance the PFR accuracy.

In the similar manner, we explore the impact of $K_p$ and $K_s$ on the F92 in two different experiments. First, we set the value of $K_p = 1$ and in 10 different experiments, increase the value of $K_s$ from 1 to 10 (Figure 5.a). As we can see, increasing $K_s$ monotonically increases the prediction accuracy until $K_s = 7$ and then the prediction accuracy remains almost similar (slightly drops). Therefore, we set $K_s = 7$. In a different experiment, we set the value of $K_s = 7$ and in 10 different experiments, increase the value of $K_p$ from 1 to 10. As we can see in Figure 5.b, different to the EDD and TG data sets, the prediction accuracy for the F92 by increasing the $K_p$ until $K_p = 7$ increases and then the (increasing $K_p/K_s$ from 7 to 10) prediction performance remains unchanged. As it is shown in Figures 5.a and 5.b, similar results are achieved for the F110 data set as well.

As it was discussed earlier, the number of folds investigated in the F92 and F110 are significantly higher than the number of folds explored in the EDD and TG data sets (over three times). The difference between the number of features (from 388 to 943) used for the EDD and TG data sets compared to the F92 and F110 data sets to provide more effective features indicates that by increasing the complexity of the problem, the amount of discriminatory information for classification task needs to be increased as well. Therefore, the number of folds explored in the employed data set can be considered as a parameter that impact on the segmentation factors to extract segmentation based features from PSSM and
SPINE-M. For this case, having up to 110 folds we are able to provide effective discriminative information by adjusting \( K_p \) and \( K_s \) both to 7. Note that, this number of features is still much lower than the number of features used in [28] and [29] to reveal effective discriminatory information. Therefore, for the rest of this study, \( K_p \) and \( K_s \) are set to 1 and 10 respectively for the EDD and TG data sets as representatives of the data sets with limited number of folds (less than 30 folds) while they are both set to 7 for the F92 and F110 as representatives of the data sets with significantly higher number of folds and consequently more complex cases (up to 110 folds).

4.2 Determining the Effect of the Proposed Feature Groups on the Protein Fold Prediction Accuracy

In continuation, we investigate the effectiveness of each of the feature groups used in this study separately to our reported protein fold prediction accuracy. The results for the EDD and TG data sets (in which \( K_p = 1 \) and \( K_s = 10 \)) are shown in Table 1 and the results for the F92 and F110 data sets (in which \( K_p = 7 \) and \( K_s = 7 \)) are shown in Table 2. As we can see, for both of the Tables 1 and 2, all the feature groups used to reveal global and local discriminatory information are effectively contribute to the achieved protein fold prediction enhancement. It shows that the protein fold prediction enhancement reported here is dependent on the all of the feature groups proposed in this study.

4.3 Comparison with the Existing Methods

We compare the results achieved by applying SVM to the combination of features proposed in this study (\( F_{global}, \) PSSM-SAC, PSSM-SD, SPINE-SAC, SPINE-SD where \( K_p \) and \( K_s \) are set to 1 and 10 respectively for the EDD and TG data sets and both are set to 7 for the F92 and F110) which will be referred as PSSM-SPINE-S (388 and 943 features in total for the EDD/TG and F92/F110 data sets) with the best results reported in the literature. The results are shown in the Tables 3 and 4. As we can see in Table 2, we report up to 73.8% and 88.2% prediction accuracy...
TABLE 1: The impact of proposed feature groups proposed in this study (using SVM classifier) to enhance protein fold prediction accuracy (in %) for the EDD, TG, F92, and F110 data sets. For EDD and TG data sets and in PSSM-SAC and SPINE-SAC feature vectors, the values of $K_p$ and $K_s$ are set to 1 and 10 respectively while for the F92 and F110 feature vectors, these two values ($K_p$ and $K_s$) are both set to 7.

<table>
<thead>
<tr>
<th>Combination of features</th>
<th>EDD</th>
<th>TG</th>
<th>F92</th>
<th>F110</th>
</tr>
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<tbody>
<tr>
<td>$F_p$global + PSSM-SD</td>
<td>74.7</td>
<td>55.7</td>
<td>64.8</td>
<td>64.1</td>
</tr>
<tr>
<td>$F_p$global + SPINE-SD</td>
<td>79.4</td>
<td>62.6</td>
<td>72.6</td>
<td>72.2</td>
</tr>
<tr>
<td>$F_p$global + PSSM-SAC</td>
<td>79.1</td>
<td>63.6</td>
<td>69.1</td>
<td>68.9</td>
</tr>
<tr>
<td>$F_p$global + SPINE-SAC</td>
<td>82.3</td>
<td>66.7</td>
<td>74.1</td>
<td>73.1</td>
</tr>
<tr>
<td>$F_p$global + PSSM-SD + SPINE-SD</td>
<td>80.1</td>
<td>64.0</td>
<td>77.6</td>
<td>77.1</td>
</tr>
<tr>
<td>$F_p$global + SPINE-SAC</td>
<td>84.1</td>
<td>68.2</td>
<td>72.9</td>
<td>72.4</td>
</tr>
<tr>
<td>$F_p$global + PSSM-SAC + SPINE-SAC</td>
<td>86.1</td>
<td>71.8</td>
<td>79.9</td>
<td>79.9</td>
</tr>
<tr>
<td>$F_p$global + PSSM-SD + SPINE-SAC + PSSM-SAC</td>
<td>87.5</td>
<td>72.6</td>
<td>79.1</td>
<td>78.7</td>
</tr>
<tr>
<td>$F_p$global + PSSM-SD + SPINE-SAC + SPINE-SAC</td>
<td>87.5</td>
<td>72.6</td>
<td>79.1</td>
<td>78.7</td>
</tr>
<tr>
<td>PSSM-SD + SPINE-SD + PSSM-SAC + SPINE-SAC</td>
<td>85.9</td>
<td>71.1</td>
<td>80.3</td>
<td>79.9</td>
</tr>
<tr>
<td>PSSM-SD + SPINE-SD + PSSM-SAC + SPINE-SAC</td>
<td>88.2</td>
<td>73.8</td>
<td>81.4</td>
<td>80.7</td>
</tr>
</tbody>
</table>

TABLE 2: Comparison of the results reported for the EDD, TG, F92, and F110 data sets (in %). Note that column named No. is referring to the number of features. For EDD and TG data sets and in PSSM-SAC and SPINE-SAC feature vectors, the values of $K_p$ and $K_s$ are set to 1 and 10 respectively while for the F92 and F110 data sets, these two values ($K_p$ and $K_s$) are both set to 7.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Features</th>
<th>No.</th>
<th>Method</th>
<th>EDD</th>
<th>TG</th>
<th>F92</th>
<th>F110</th>
</tr>
</thead>
<tbody>
<tr>
<td>[40]</td>
<td>AAO (from original protein sequence)</td>
<td>20</td>
<td>LDA</td>
<td>46.9</td>
<td>36.3</td>
<td>32.7</td>
<td>31.3</td>
</tr>
<tr>
<td>[40]</td>
<td>AAC (from original protein sequence)</td>
<td>20</td>
<td>LDA</td>
<td>40.9</td>
<td>32.0</td>
<td>30.2</td>
<td>29.6</td>
</tr>
<tr>
<td>[19]</td>
<td>Physicochemical Features + AAC</td>
<td>125</td>
<td>SVM</td>
<td>50.1</td>
<td>39.5</td>
<td>39.1</td>
<td>38.4</td>
</tr>
<tr>
<td>[33]</td>
<td>Physicochemical Features + AAC</td>
<td>220</td>
<td>ANN(RBF)</td>
<td>52.8</td>
<td>41.9</td>
<td>43.4</td>
<td>41.9</td>
</tr>
<tr>
<td>[44]</td>
<td>Threading</td>
<td>-</td>
<td>Naive Bayes</td>
<td>70.3</td>
<td>55.3</td>
<td>56.3</td>
<td>54.8</td>
</tr>
<tr>
<td>[3]</td>
<td>FF (bi-gram)</td>
<td>400</td>
<td>SVM</td>
<td>75.2</td>
<td>52.7</td>
<td>60.2</td>
<td>59.5</td>
</tr>
<tr>
<td>[3]</td>
<td>TF (tri-gram)</td>
<td>8000</td>
<td>SVM</td>
<td>71.0</td>
<td>49.4</td>
<td>63.2</td>
<td>62.1</td>
</tr>
<tr>
<td>[29]</td>
<td>Combination of bi-gram features</td>
<td>2400</td>
<td>SVM</td>
<td>69.9</td>
<td>55.0</td>
<td>69.9</td>
<td>55.0</td>
</tr>
<tr>
<td>[21]</td>
<td>PSIPRED and PSSM features</td>
<td>242</td>
<td>SVM</td>
<td>77.5</td>
<td>60.1</td>
<td>70.5</td>
<td>68.8</td>
</tr>
<tr>
<td>[26]</td>
<td>ACCold-AC</td>
<td>200</td>
<td>SVM</td>
<td>80.1</td>
<td>58.8</td>
<td>68.2</td>
<td>68.0</td>
</tr>
<tr>
<td>[26]</td>
<td>ACCold-ACC</td>
<td>4000</td>
<td>SVM</td>
<td>85.9</td>
<td>66.4</td>
<td>78.2</td>
<td>77.3</td>
</tr>
<tr>
<td>This study</td>
<td>PSSM-SPINE-S</td>
<td>388</td>
<td>SVM</td>
<td>88.2</td>
<td>73.8</td>
<td>81.4</td>
<td>80.7</td>
</tr>
</tbody>
</table>

accuracies for the TG and EDD data sets respectively. These results are up to 7.4% and 2.3% better than the highest reported results for these two data sets that are achieved by reproducing the results reported in [28] for the TG and EDD data sets (66.4% and 85.9% prediction accuracies) respectively. The enhancement achieved compared to other similar approaches to reveal more local information such as bi-gram [29] and tri-gram [3] is much more significant (over 11% for the EDD and TG data sets). The higher enhancement achieved for the TG data set compared to [28] shows that our method is more effective when the sequence similarity rate is very low (up to 25%). It is also important to highlight that we outperformed [28] using 388 features (for the EDD and TG data sets) compared to 4000 features used in that study.

Similarly, as shown in Table 3, for the first time, we report over 80% prediction accuracy for a data set that has over 100 folds. We report 81.4% and 80.7% prediction accuracies for the F92 and F110 data sets respectively. These results are up to 3.2% and 3.4% better than the highest reported results for these two data sets that are achieved by reproducing the results reported in [28] for the F92 and F110 data sets (78.2% and 77.3% prediction accuracies) respectively. It is also important to highlight that we outperformed [28] using 943 features compared to 4000 features used in that study. Despite having larger number of features (943 features) compared to the number of features used for the EDD and TG data sets (388 features), it is still dramatically lower than the number of features used in the state-of-the-art methods used for the PFR. We have also conducted pairwise t-test to investigate the statistical significance of our reported results. The probability value calculated for the pairwise t-test ($p = 0.001$) emphasizes the statistical significance of our reported results and the enhancement achieved in this study. In result, our proposed methodology is able to significantly enhance the protein fold prediction accuracy compared to the previous studies found in the literature and at the same time reduce the number of features used for this task significantly. In other words, we are able to provide more local and global information from PSSM and SPINE-X for the PFR compared to previously proposed approaches found in the literature.

5 Conclusion

In this study, we have proposed two novel segmentation based feature extraction techniques to reveal more local discriminatory information embedded in PSSM and SPINE-X. We also employed the concept of occurrence feature group and extend it to provide more global discriminatory information from PSSM and SPINE-X for the PFR compared to previously used methods for this task. We have used four data sets namely, the EDD, TG, F92, and F110 have been used to investigate the impact of our proposed feature extraction methods. These data sets enabled us to investigate the impact of our proposed methods when the sequence similarity rate was very low (TG), when larger number of folds (and consequently more complex case) was used (F92, and F110), and to directly compare our results with the state-of-the-art methods found in the literature (EDD). By applying SVM to the combination of our extracted features we significantly enhanced protein fold prediction accuracy compared to previously reported results in the literature.
For the EDD and TG data sets, we achieved up to 73.8% and 88.2% prediction accuracies, up to 7.4% and 2.3% better than previous results found in the literature, respectively [28]. These enhancements were achieved by using less than 1/10 of the number of features used previously in [28].

By investigating the PFR using the F92 and F110 data sets, we showed that by increasing the number of folds the complexity of the problem is increasing and therefore, more discriminatory information is required to tackle this problem. We also showed by using segmentation based feature extraction technique, we are able to tackle this problem as well and enhance the protein fold prediction accuracy. For the first time, we reported over 80% prediction accuracy for a data set containing proteins belonging to over 100 folds. We achieved to over 80% and 80.7% prediction accuracies for the F92, and F110 data sets respectively, up to 3.2% and 3.4% better than previous studies found in the literature [28] using F110 data sets respectively, up to 3.2% and 3.4% better than previous results found in the literature, up to 3.2% and 3.4% better than previous studies found in the literature [28] using F110 data sets respectively, up to 3.2% and 3.4% better than previous results found in the literature [28].

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REFERENCES


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